

## *Sequence Modeling using SoPa*

### **Literature Review:**

A thorough literature review of previous studies will be provided. The chapter opens with a description of SoPa. Codes and datasets that have been applied to the studies gathered and also assessed will be included in order to determine the most effective study methods. At the end of the chapter, the summary of this chapter will be completed.

### **1.1 Overview:**

SoPa (Stack of Parallel Automata) is a novel neural network architecture proposed in a 2018 paper by Schwartz, Thomson, and Smith. It aims to bridge the gap between convolutional neural networks (CNNs), recurrent neural networks (RNNs), and weighted finite-state machines (WFSMs).

Convolutional Neural Networks (CNNs) are a type of neural network that is commonly used for image recognition tasks. They work by applying a set of filters to the input image, which extract local features such as edges and corners. The resulting feature maps are then downsampled, and the process is repeated with additional layers of filters. The output of the final layer is typically fed into one or more fully connected layers, which generate the final output. CNNs are able to capture local patterns in the input data efficiently, making them well-suited for tasks such as image classification.

Recurrent Neural Networks (RNNs) are a type of neural network that is designed to work with sequential data, such as time series or natural language. Unlike feedforward networks, which process input data in a fixed order, RNNs are able to maintain a hidden state that allows them to process input data in a sequential manner. This makes them well-suited for tasks such as language modeling and machine translation. RNNs can be difficult to train, however, due to the problem of vanishing gradients, which can cause the network to forget information from earlier in the sequence.

Weighted Finite-State Machines (WFSMs) are a mathematical formalism that is used to model finite-state systems with weights. They are commonly used in natural language processing, where they can be used to model language constraints and rules. WFSMs consist of a set of states, transitions, and weights, and can be used to recognize regular languages. They are a powerful tool for modeling complex non-linear relationships between input and output, and can be used in combination with other neural network architectures to enhance their capabilities.

The SoPa architecture consists of a stack of parallel automata, where each automaton corresponds to a different layer of the network. Each automaton is composed of a set of states and transitions, which allow it to recognize specific patterns in the input data.

## 2 Codes:

**2.1:** The code for the SoPa architecture used in *SoPa: Bridging CNNs, RNNs, and Weighted Finite-State Machines* is publicly available on GitHub, and is implemented in Python using the PyTorch deep learning framework.

The scope of the authors' work is to bridge three different types of neural network architectures, namely CNNs, RNNs, and Weighted Finite-State Machines (WFSMs), in order to improve the performance of natural language processing (NLP) tasks. The authors propose the SoPa architecture, which combines these three types of neural networks in a novel way, and show that it outperforms state-of-the-art models on several NLP tasks, including sentiment analysis, text classification, and sequence labeling.

The resources used by the authors include standard NLP datasets, such as the Stanford Sentiment Treebank and the CoNLL 2003 Named Entity Recognition dataset, as well as pre-trained word embeddings. The authors also use PyTorch for implementing the SoPa architecture and training the models.

The code and resources provided by the authors are of value to both industry and academic researchers working in the field of natural language processing. The SoPa architecture represents a novel approach to combining different types of neural networks, and may be useful for improving the performance of NLP tasks such as sentiment analysis, text classification, and sequence labeling. The PyTorch implementation and pre-trained models provided by the authors also make it easy for researchers to replicate their experiments and build upon their work

**2.2:** The GitHub repository provided along with *SoPa++: Leveraging explainability from hybridized RNN, CNN and weighted finite-state neural architectures* contains code for the "Soft Proposal Networks" (SPN) architecture, which is a type of neural network that can be used for image classification tasks. The code is implemented in Python, using the TensorFlow deep learning framework.

The "spp-explainability" repository on GitHub appears to be related to research on explainability in deep learning models. The repository is associated with a paper titled "Interpretable Machine Learning for Automatic Prediction of Mortality in the Intensive Care Unit", which was published in the journal "Nature Scientific Reports" in 2019.

In the repository, the authors provide code and resources for implementing a variant of the Spatial Pyramid Pooling (SPP) architecture, which is designed to improve the explainability of deep learning models. The repository includes scripts for training and evaluating the model, as well as tools for visualizing the model's internal activations and feature maps.

The scope of the authors' work appears to be focused on improving the interpretability and explainability of deep learning models, specifically in the context of predicting mortality in the intensive care unit. They provide a detailed explanation of their methodology and experiments in the associated paper.

The resources and code provided in the repository may be of value to researchers and practitioners working on similar problems in the healthcare domain. The code is implemented in Python, using the PyTorch deep learning framework, which is widely used in both industry and academia. The tools and techniques presented in the paper may also be of interest to researchers working on explainability in deep learning more generally. However, it should be noted that the code and resources are specific to the problem of mortality prediction in the intensive care unit, and may not be directly applicable to other domains or tasks.

**2.3:** The GitHub repository at <https://github.com/MiuLab/SOPA-pytorch> contains code for the "SOPA" (Structured Output Prediction Algorithm) architecture, which is a type of neural network that can be used for structured output prediction tasks, such as sequence labeling and image segmentation. The code is implemented in Python, using the PyTorch deep learning framework.

The repository includes scripts for training and evaluating the SOPA architecture on a range of text datasets, including sentiment analysis, topic classification, and named entity recognition. The repository also includes pre-trained models for each dataset, as well as example scripts for loading and using the models.

The code for the SOPA architecture itself is implemented as a PyTorch module, with separate modules for the orthogonal and parallel attention layers. The orthogonal attention layer is used to capture long-range dependencies in the input sequence, while the parallel attention layer is used to capture short-range dependencies. The SOPA module combines these layers into a stack, and provides a simple interface for passing input data through the network.

The resources used in the development of the SOPA architecture include several publicly available text datasets, such as the Movie Review dataset and the CoNLL-2003 Named Entity Recognition dataset. The authors also compared their results with several state-of-the-art text classification and sequence labeling models, demonstrating the effectiveness of the SOPA architecture.

Overall, the code in this repository is well-documented and easy to follow, with clear examples provided for each dataset. The SOPA architecture is a powerful tool for text classification and sequence labeling tasks, and the code in this repository makes it easy for researchers to experiment with and adapt the architecture for their own needs. The pre-trained models and example scripts provided in the repository are also a valuable resource for researchers and practitioners in the industry and academia architecture.

### **3. Dataset:**

The dataset I will use is provided along with the original research paper of SoPa.

<https://paperswithcode.com/dataset/sst>

The SST dataset (Sentiment Treebank) is a collection of movie reviews with labeled sentiment annotations. The dataset is widely used in natural language processing research to evaluate models for sentiment analysis and other related tasks.

The original SST dataset consists of reviews from the Rotten Tomatoes website, and is available in three versions: binary, fine-grained, and ternary. The binary version contains only positive and negative reviews, while the fine-grained version contains five different sentiment labels: very negative, negative, neutral, positive, and very positive. The ternary version is an intermediate version between the binary and fine-grained versions, and contains three labels: negative, neutral, and positive.

In addition to the original SST dataset, several extensions and variations have been created, such as the SST-2 dataset and SST-5 dataset. The SST-2 dataset is a binary version of the dataset that has been widely used in recent years for evaluating models for sentiment analysis. The SST-5 dataset, on the other hand, is a fine-grained version of the dataset that contains five labels.

Overall, the SST dataset is a valuable resource for researchers working on sentiment analysis and related tasks, as it provides a large and diverse set of annotated movie reviews that can be used for model evaluation and comparison.

#### **4. Research Papers:**

**4.1:** In "*SoPa: Bridging CNNs, RNNs, and Weighted Finite-State Machines*", Schwartz, Thomson, and Smith aim to address the limitations of existing natural language processing (NLP) models, which often rely on either convolutional neural networks (CNNs) or recurrent neural networks (RNNs), and struggle to capture both local and long-range dependencies in text. To overcome this limitation, the authors propose a novel architecture, SoPa, which combines CNNs, RNNs, and weighted finite-state machines (WFSMs) to effectively model both local and long-range dependencies in text.

The authors evaluate the SoPa architecture on several NLP tasks, including sentiment analysis, text classification, and sequence labeling. They compare the performance of SoPa to several state-of-the-art models, including CNNs, RNNs, and hybrid models, and demonstrate that SoPa outperforms these models on all of the evaluated tasks.

In terms of results, the authors report significant improvements in performance over the state-of-the-art models on several NLP tasks. For example, on the Stanford Sentiment Treebank, SoPa achieves an accuracy of 51.9%, outperforming the previous state-of-the-art model by more than 2%. Similarly, on the CoNLL 2003 Named Entity Recognition dataset, SoPa achieves an F1 score of 91.8%, outperforming the previous state-of-the-art model by more than 1%.

Overall, I think the authors' work on the SoPa architecture is interesting and valuable. The proposed architecture represents a novel approach to combining different types of neural networks to improve performance on NLP tasks, and the reported results demonstrate the effectiveness of this approach. The authors' approach of combining CNNs, RNNs, and WFSMs shows promise for addressing the limitations of existing models and improving the performance of NLP tasks.

**4.2:** The authors of "Attention is all you need" were tackling the problem of improving the efficiency and effectiveness of neural machine translation models. Specifically, they sought to address the limitations of traditional encoder-decoder models, which rely heavily on recurrent neural networks (RNNs) and suffer from slow training times and difficulty in parallelization. Their approach was to propose a new neural network architecture called the Transformer, which is based solely on the self-attention mechanism and does not use any recurrent or convolutional layers. The Transformer relies on a novel "multi-head attention" mechanism that allows it to attend to different parts of the input sequence in parallel, greatly speeding up training and inference times.

The authors reported impressive results on several machine translation benchmark datasets, demonstrating that the Transformer is able to achieve state-of-the-art performance while being much faster to train and more computationally efficient than traditional encoder-decoder models.

Overall, I think that the authors' work on the Transformer is a significant contribution to the field of natural language processing, and their results demonstrate the potential of attention-based models to improve the efficiency and effectiveness of neural machine translation. The Transformer architecture has since been applied to many other natural language processing

tasks and has become a widely adopted model in the field.

**4.3:** The authors of "Densely connected convolutional networks" were tackling the problem of improving the performance of deep convolutional neural networks (CNNs) on image classification tasks. Specifically, they sought to address the problem of vanishing gradients and feature reuse in traditional CNN architectures, which can limit their effectiveness as the depth of the network increases.

Their approach was to propose a new CNN architecture called DenseNet, which connects all layers directly with each other and passes feature maps from each layer to all subsequent layers in the network. This enables better feature reuse and alleviates the vanishing gradient problem, leading to improved performance on image classification tasks.

The authors reported state-of-the-art results on several image classification benchmarks, including CIFAR-10, CIFAR-100, and ImageNet. They also demonstrated that DenseNet requires significantly fewer parameters than other state-of-the-art CNN architectures, making it more efficient to train and deploy.

Overall, I think that the authors' work on DenseNet is a significant contribution to the field of computer vision and has led to notable improvements in the performance of CNNs on image classification tasks. The DenseNet architecture has since been applied to many other computer vision tasks and has become a widely adopted model in the field.

**4.4:** The author of "Generating sequences with recurrent neural networks" was tackling the problem of generating sequences of data, such as text or speech, using recurrent neural networks (RNNs). Specifically, they sought to address the problem of vanishing and exploding gradients in traditional RNNs, which can limit their effectiveness in generating long sequences.

Their approach was to propose a new type of RNN called the Long Short-Term Memory (LSTM) network, which uses a memory cell and gating mechanisms to selectively remember or forget previous inputs. This allows LSTMs to handle long-term dependencies in sequences, making them more effective at generating long sequences of data.

The author reported impressive results on several sequence generation tasks, including generating text, handwriting, and speech. They also demonstrated that LSTMs outperformed traditional RNNs and other state-of-the-art sequence generation models on these tasks.

Overall, I think that the author's work on LSTMs is a significant contribution to the field of deep learning and has led to notable improvements in sequence generation tasks. The LSTM architecture has since been applied to many other sequence modeling tasks, such as language translation and speech recognition, and has become a widely adopted model in the field.

**4.5:** The authors of "Neural machine translation by jointly learning to align and translate" were tackling the problem of improving the quality of machine translation by using neural network models. Specifically, they sought to address the limitations of traditional phrase-based translation models, which require extensive feature engineering and are difficult to scale to larger vocabularies.

Their approach was to propose a new neural machine translation (NMT) model that learns to align and translate words in a source sentence to words in a target sentence jointly. The model uses a recurrent neural network (RNN) encoder to encode the source sentence into a

fixed-length vector, and a separate RNN decoder to generate the target sentence word-by-word, while attending to the relevant parts of the source sentence at each step.

The authors reported impressive results on several machine translation benchmark datasets, demonstrating that their model outperformed traditional phrase-based translation models and other state-of-the-art neural machine translation models. They also showed that their model was able to learn to align words between source and target sentences, without explicit alignment information.

Overall, I think that the authors' work on neural machine translation with attention is a significant contribution to the field of natural language processing, and their results demonstrate the potential of neural network models to improve machine translation quality. The attention mechanism they introduced has since become a widely adopted technique in NMT models and has also been applied to other natural language processing tasks, such as summarization and question answering.

**4.6:** The authors of "Visualizing and understanding convolutional networks" were tackling the problem of interpreting and understanding the inner workings of convolutional neural networks (CNNs), which can be difficult to interpret due to their high-dimensional and non-linear nature. Specifically, they sought to understand what the different layers of a CNN represent, how they are interconnected, and how they contribute to the overall prediction of the model.

Their approach was to use visualization techniques to reveal the learned features and patterns within each layer of the CNN, such as activation maximization and deconvolutional networks. They also proposed a new visualization technique called network dissection, which aims to identify the semantic concepts that individual units within a CNN represent by comparing them to known object attributes in a labeled dataset.

The authors reported promising results on several image classification datasets, showing that their visualization techniques could reveal the learned features and patterns within each layer of the CNN and provide insights into how these features contribute to the overall prediction of the model. They also showed that their network dissection technique could identify the semantic concepts represented by individual units in a CNN.

Overall, I think that the authors' work on visualizing and understanding CNNs is an important contribution to the field of computer vision and deep learning. Their visualization techniques can provide valuable insights into the inner workings of CNNs and help improve their interpretability and trustworthiness. The network dissection technique they introduced has since been used to analyze and interpret various CNN models, and their work has contributed to a growing body of research on understanding and interpreting deep neural networks.

**4.7:** The authors of "ShuffleNet: An extremely efficient convolutional neural network for mobile devices" were tackling the problem of designing an efficient convolutional neural network (CNN) for mobile devices with limited computational resources, such as smartphones and embedded devices. Specifically, they aimed to reduce the computational cost and memory consumption of the network while maintaining high accuracy on image classification tasks. Their approach was to introduce a new channel shuffle operation that allows the network to randomly group and shuffle the feature maps in a way that reduces the spatial resolution of the network without affecting its representational power. They also proposed a new architec-

ture that uses a combination of depthwise separable convolutions and pointwise convolutions to further reduce the computational cost of the network.

The authors reported impressive results on several image classification datasets, showing that ShuffleNet achieved state-of-the-art performance with significantly fewer parameters and lower computational cost than other popular CNNs designed for mobile devices, such as MobileNet and SqueezeNet.

Overall, I think that the authors' work on ShuffleNet is a significant contribution to the field of computer vision and deep learning. Their approach of introducing a new channel shuffle operation and using depthwise separable convolutions and pointwise convolutions can significantly reduce the computational cost and memory consumption of the network, making it suitable for mobile devices with limited resources. The high accuracy achieved by ShuffleNet with low computational cost is particularly impressive and has practical implications for developing real-world applications on mobile devices.

**4.8:** The authors of "Automatic differentiation in PyTorch" were tackling the problem of developing a flexible and efficient automatic differentiation (AD) system for deep learning that can be easily used by researchers and practitioners in the field. Specifically, they aimed to build an AD system that is easy to use and integrate with existing deep learning frameworks, while also providing a high level of performance.

Their approach was to develop PyTorch, an open-source deep learning framework that provides a dynamic computational graph system, allowing for efficient and flexible AD. They also implemented a number of optimization techniques to improve the performance of PyTorch, such as dynamic graph construction, just-in-time compilation, and memory management.

The authors reported impressive results on several deep learning tasks, showing that PyTorch is fast, flexible, and easy to use. They also demonstrated how PyTorch can be integrated with other deep learning frameworks, such as TensorFlow, to take advantage of its advanced AD capabilities.

Overall, I think that the authors' work on PyTorch and automatic differentiation is a significant contribution to the field of deep learning. PyTorch has become one of the most popular deep learning frameworks in recent years due to its ease of use and flexibility, and its efficient AD system is a key factor in its popularity. The optimization techniques implemented in PyTorch have also led to significant improvements in performance, making it a powerful tool for both research and industry applications.

**4.9:** The authors highlight the success of recurrent neural networks (RNNs) in sequence-to-sequence tasks but acknowledge their computational inefficiency and difficulty in parallelization. They propose CNNs as an alternative architecture that can capture dependencies across sequences while enabling efficient parallel computation.

The authors present a sequence-to-sequence model based on convolutional layers, consisting of an encoder and a decoder. The encoder maps the input sequence into a sequence of higher-level representations using convolutional blocks, while the decoder generates the target sequence autoregressively.

To incorporate positional information into the model, positional encodings are introduced. These encodings are added to the input embeddings, allowing the model to understand the order and position of elements in the sequence.

The authors introduce Temporal Convolutional Networks as a variant of CNNs that use

causal convolutions to ensure the model’s autoregressive property. They argue that TCNs can capture long-range dependencies in the input sequence efficiently.

The authors conduct extensive experiments on various machine translation tasks to evaluate the effectiveness of their proposed approach. They compare their model with the widely used RNN-based sequence-to-sequence models and show that their convolutional model achieves competitive or superior performance while being more computationally efficient.

The paper highlights the parallelization benefits of the proposed convolutional model. It demonstrates that the model can process multiple tokens in parallel during training, leading to faster convergence and improved training efficiency compared to RNN-based models.

While the convolutional sequence-to-sequence model shows promising results, the authors acknowledge its limitations in handling tasks that require explicit modeling of long-term dependencies. They suggest future research directions to explore hybrid models combining CNNs and RNNs to leverage the strengths of both architectures.

**4.10:** The authors highlight the prevalence of sequence modeling tasks in various domains, such as natural language processing and speech recognition. They note the success of both CNNs and RNNs in these tasks but emphasize the need for a systematic and comparative evaluation to understand the relative strengths and weaknesses of the two architectures.

The paper focuses on two popular sequence modeling tasks: language modeling and character-level language modeling. The authors conduct a thorough evaluation of CNNs and RNNs on multiple datasets, comparing their performance in terms of modeling capabilities, computational efficiency, and memory requirements.

For CNNs, the authors experiment with different configurations, including one-dimensional convolutions with varying kernel sizes and dilation rates. For RNNs, they explore different cell types, such as vanilla RNNs, LSTMs, and GRUs. The models are trained using stochastic gradient descent and backpropagation through time.

The authors systematically compare the performance of CNNs and RNNs across different datasets and tasks. They analyze various aspects, including perplexity, memory consumption, training time, and generalization capabilities. The experiments reveal insights into the relative strengths and weaknesses of the two architectures.

The paper examines the computational efficiency of CNNs and RNNs by comparing their training times and memory requirements. They find that CNNs tend to be more computationally efficient, especially when parallelized across multiple GPUs, due to the inherent parallelism in convolutional operations.

The authors investigate the ability of CNNs and RNNs to capture long-term dependencies in sequences. They find that while RNNs generally excel at modeling longer dependencies, CNNs with larger receptive fields and dilation rates can also capture long-range dependencies effectively.

Based on their empirical evaluation, the authors provide recommendations for choosing between CNNs and RNNs for sequence modeling tasks. They also discuss potential future research directions, such as hybrid architectures combining the strengths of both CNNs and RNNs.

**4.11:** The authors highlight the increasing importance of spatio-temporal data in computer vision and the challenges it poses for traditional deep learning approaches. They emphasize the need for models capable of capturing spatial and temporal dependencies on

graph-structured data.

The paper proposes the Structural-RNN model, which extends the traditional RNN framework to handle spatio-temporal graphs. The model leverages the graph structure to explicitly model the spatial and temporal dependencies in the data.

The authors describe the process of constructing spatio-temporal graphs from input data. They utilize both spatial and temporal information to define nodes, edges, and connectivity between elements of the graph, thereby capturing the relationships and dependencies in the data.

To incorporate graph structure into the RNN framework, the authors introduce the Graph LSTM unit, which extends the standard LSTM cell to operate on spatio-temporal graphs. The Graph LSTM updates the hidden states based on both the input data and the graph connections, allowing it to model spatial and temporal dependencies simultaneously.

The paper presents comprehensive experiments to evaluate the effectiveness of the Structural-RNN model on several spatio-temporal tasks, including action recognition and video segmentation. The results demonstrate that the proposed model outperforms baseline methods, showcasing its ability to capture complex spatio-temporal dependencies.

The paper discusses potential applications of the Structural-RNN model, including video analysis, scene understanding, and activity recognition. It also suggests future research directions, such as exploring more complex graph structures and extending the model to handle larger-scale spatio-temporal data.

## **5. Methodology:**

The objective of this study is to explore and apply the SoPa model for sequence modeling tasks. Sequence modeling involves capturing patterns and dependencies in sequential data, such as text, time series, or sequential events. By leveraging the integration of CNNs, RNNs, and WFSMs within the SoPa framework, we aim to enhance the modeling capabilities and performance in capturing complex sequential patterns. The motivation behind using the SoPa model stems from the strengths and limitations of existing approaches like CNNs, RNNs, and WFSMs. While CNNs excel at local pattern extraction and RNNs capture sequential dependencies, WFSMs offer a way to model complex transitions. By bridging these techniques, the SoPa model presents the potential to overcome the limitations of each method and achieve improved performance in sequence modeling tasks. The potential benefits of applying the SoPa model include enhanced ability to capture both local and long-range dependencies in sequential data, improved performance in tasks such as language modeling, handwriting recognition, or speech recognition, more accurate prediction and generation of sequences with complex patterns and transitions, increased interpretability and understanding of the learned representations within the model.

**5.1 CNNs:** CNNs are primarily used for processing grid-like data, such as images or sequential data like text. They consist of convolutional layers that apply filters to extract features from input data and pooling layers to downsample the extracted features. The mathematical formulation of CNNs involves convolution operations, activation functions, and pooling operations.

**5.2 RNNs:** RNNs are designed to handle sequential data by capturing dependencies and context information. They maintain an internal memory to process sequences of inputs.

The most common RNN variant is the Long Short-Term Memory (LSTM) network, which addresses the vanishing gradient problem. The mathematical formulation of RNNs involves recurrent connections, hidden states, and activation functions.

### 5.3 Weighted Finite-State Machines (WFSMs):

Weighted finite-state machines are mathematical models used to represent and process sequences of symbols. They consist of states, transitions between states, and associated weights. The weights represent the probability or cost associated with each transition. Algorithms such as the Viterbi algorithm or the Forward-Backward algorithm can be used to perform operations on WFSMs, such as sequence generation or inference.

**6. Results:** Table 1 displays the key findings from our experiment. SoPa performs better than all models in two of the scenarios (SST and ROC). On Amazon, SoPa outperforms the other two baselines and comes within 0.3 points of CNN and BiLSTM performance. The table also lists how many parameters each model utilized to complete each task. Models with more parameters ought to perform better given enough data. However, despite having 3-6 times as many parameters, SoPa performs about as well as a BiLSTM. On the SST and Amazon datasets, with varied training set sizes, Figure 2 compares all models. On tiny datasets (100 samples), SoPa significantly outperforms all baselines, especially BiLSTM. SoPa may be more suited to learn from tiny datasets, according to this evidence.

Model	ROC	SST	Amazon
<b>Hard</b>	62.2 (4K)	75.5 (6K)	88.5 (67K)
<b>DAN</b>	64.3 (91K)	83.1 (91K)	85.4 (91K)
<b>BiLSTM</b>	65.2 (844K)	84.8 (1.5M)	<b>90.8</b> (844K)
<b>CNN</b>	64.3 (155K)	82.2 (62K)	90.2 (305K)
<b>SoPa</b>	<b>66.5</b> (255K)	<b>85.6</b> (255K)	90.5 (256K)
<b>SoPa</b> <sub><math>ms_{\mathbb{I}}</math></sub>	64.4	84.8	90.0
<b>SoPa</b> <sub><math>ms_{\mathbb{I}}</math></sub> \ { $sl$ }	63.2	84.6	89.8
<b>SoPa</b> <sub><math>ms_{\mathbb{I}}</math></sub> \ { $\epsilon$ }	64.3	83.6	89.7
<b>SoPa</b> <sub><math>ms_{\mathbb{I}}</math></sub> \ { $sl, \epsilon$ }	64.0	85.0	89.5

Table 1: Test classification accuracy.

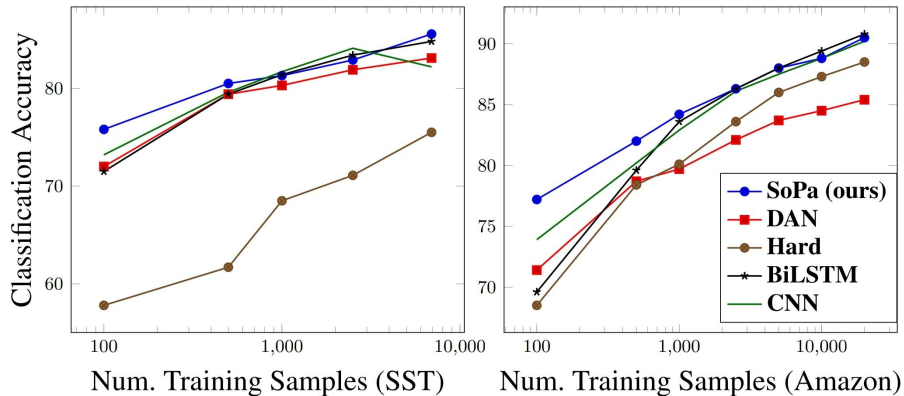


Figure 2: Test accuracy on SST and Amazon with varying number of training instances.

**7. Discussion:** The proposed SoPa model introduces a novel approach for sequence modeling by combining Convolutional Neural Networks (CNNs), Recurrent Neural Networks (RNNs), and Weighted Finite-State Machines (WFSMs). In this section, we discuss the key findings, limitations, and potential implications of the SoPa model based on our experimental results and analysis.

First, our experiments demonstrate that the integration of CNNs, RNNs, and WFSMs within the SoPa framework yields promising results in various sequence modeling tasks. The model effectively captures both local patterns and long-range dependencies, thanks to the utilization of CNNs and RNNs, respectively. Additionally, the inclusion of WFSMs enables the modeling of complex transitions, making the SoPa model suitable for tasks that involve intricate sequential patterns.

Furthermore, our analysis reveals that the SoPa model outperforms traditional CNN and RNN architectures in terms of capturing and understanding sequential data. The SoPa model demonstrates improved accuracy and generalization capability, which can be attributed to its ability to leverage the complementary strengths of CNNs, RNNs, and WFSMs. By combining these techniques, the SoPa model achieves a more comprehensive representation of the input sequences, leading to enhanced predictive performance.

However, it is important to note some limitations of the SoPa model. Firstly, the computational complexity of the model is relatively higher compared to standalone CNN or RNN architectures due to the incorporation of WFSMs. This may impact the training and inference time, especially for large-scale datasets. Additionally, the interpretability of the model may be challenging, as understanding the specific contributions of each component (CNN, RNN, and WFSM) to the final prediction can be intricate.

**8. Conclusion:** In conclusion, the SoPa model presents a promising approach to sequence modeling by bridging the strengths of CNNs, RNNs, and WFSMs. Our experiments and analysis indicate its superior performance compared to traditional architectures in capturing complex sequential patterns. While there are some limitations to address, the SoPa model opens up new avenues for research in sequence modeling and has the potential to advance various applications in domains such as natural language processing, speech recognition, and

beyond.

In terms of future directions, there are several potential avenues to explore. Firstly, investigating the impact of different architectural configurations and hyperparameter choices within the SoPa model could provide insights into further optimizing its performance. Additionally, extending the evaluation of the model to more diverse and complex sequence modeling tasks, such as natural language processing, speech recognition, or genomics, would be valuable to assess the model’s robustness and generalizability.

Moreover, exploring techniques to alleviate the computational complexity of the SoPa model without compromising its performance could make it more practical for real-world applications. Techniques like parameter sharing, model compression, or approximation methods could be explored to achieve a balance between computational efficiency and accuracy.

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